



Effects of Gravity on Supercritical Water Oxidation (SCWO) Processes

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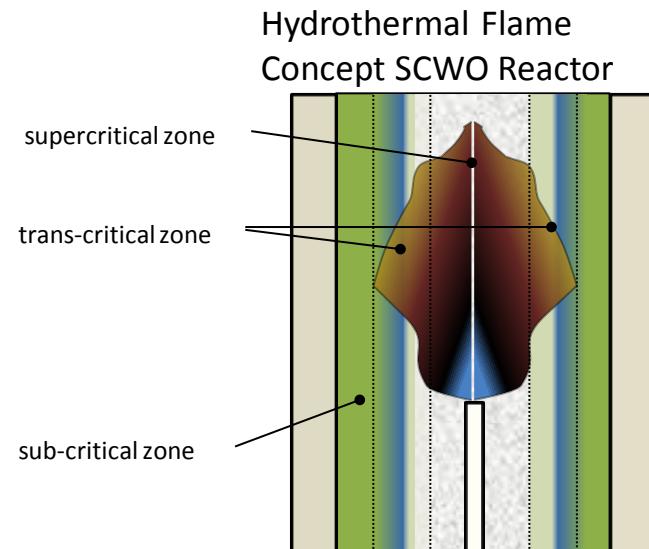
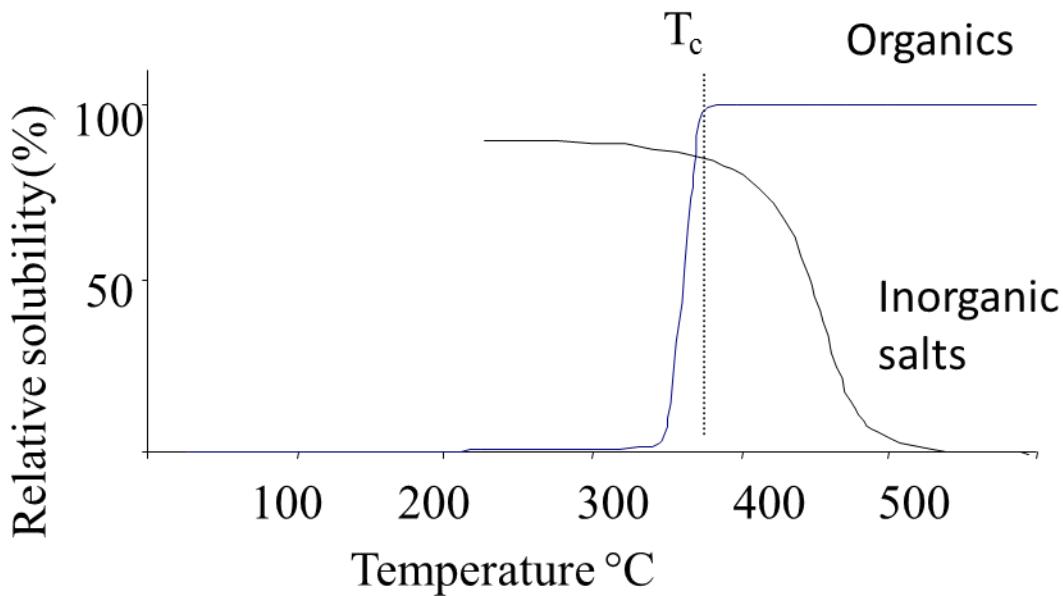
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Motivation and Application

Precursor study to the investigation of supercritical water oxidation (SCWO)

Dissolve inorganic precipitates generated during SCWO in a subcritical shroud



Objectives

- Characterize the hydrodynamics of supercritical water jets
- Identify the jet injection conditions leading to laminar and turbulent regimes
- Assess the effects of buoyancy on the jet behavior

$Re \sim \text{Momentum}/\text{Viscous}$

$$Re = \frac{\rho U d}{\mu}$$

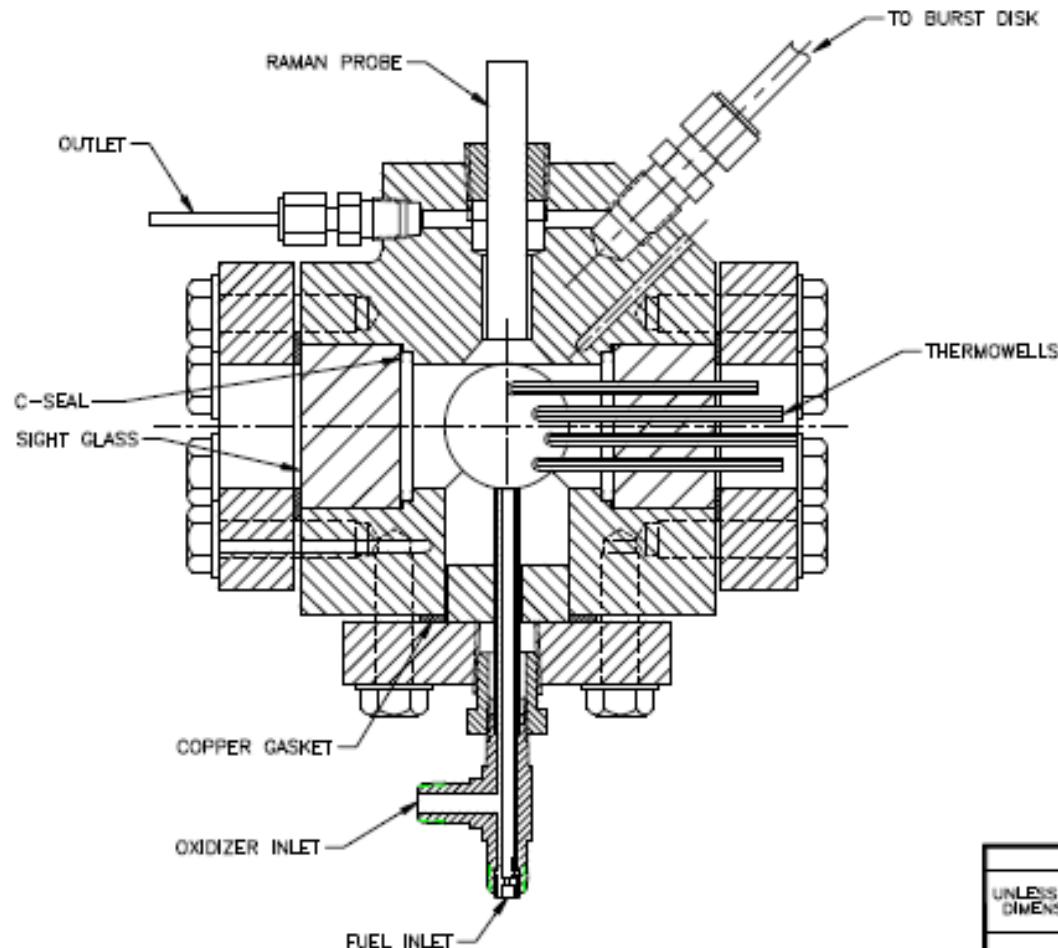
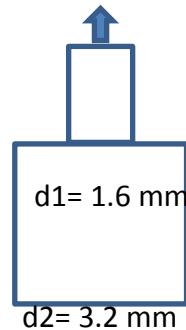
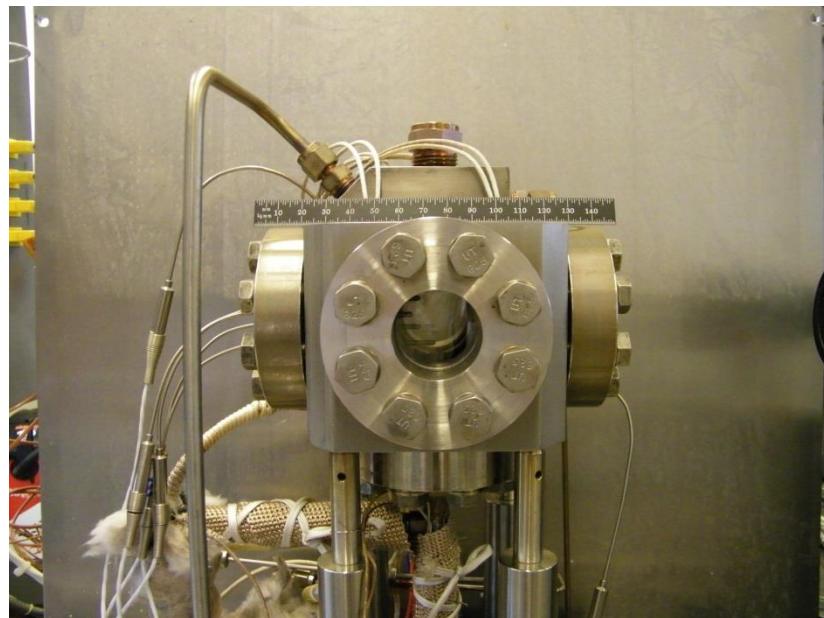
$F \sim \text{Momentum}/\text{Buoyancy}$

$$F = \frac{U}{(\frac{\Delta \rho}{\rho} g d)^{1/2}}$$

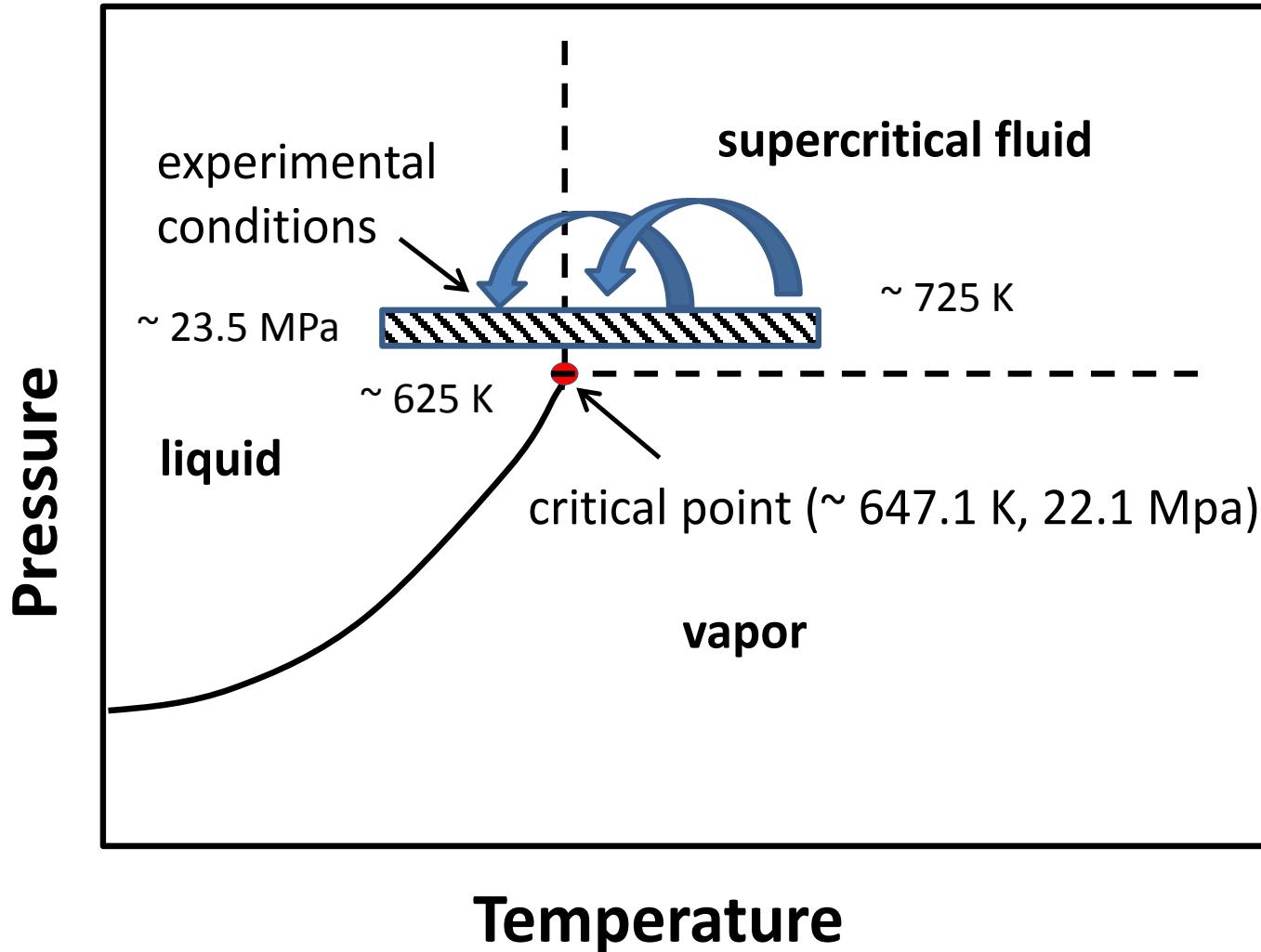
$Gr \sim \text{Buoyancy}/\text{Viscous}$

$$Gr = (\frac{Re}{F})^2$$

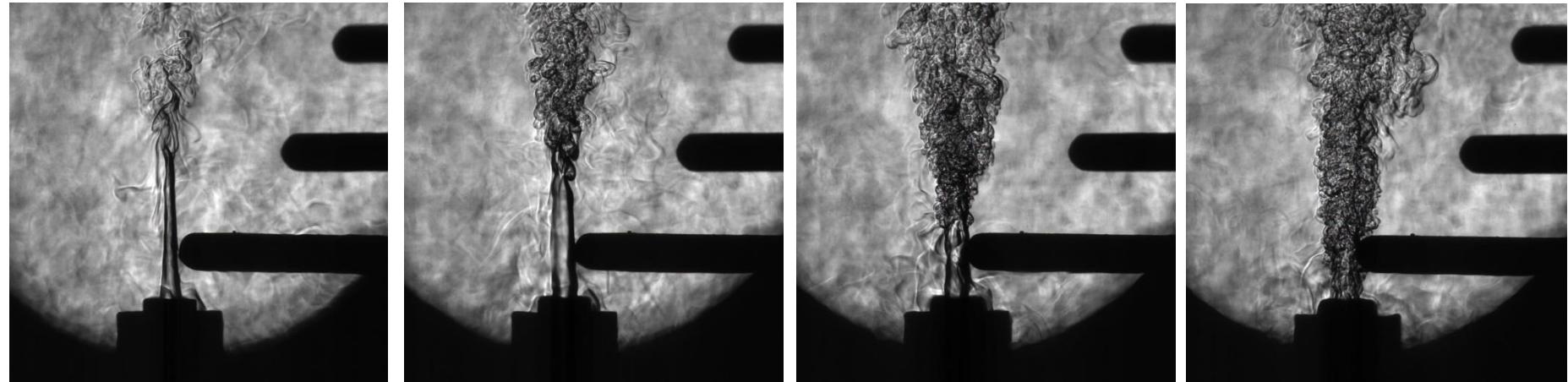
SUPERCritical WATER TEST CELL



Experimental Conditions



Supercritical Jet Injected into Supercritical Water



Re = 448
F = 1.37

Re = 1330
F = 3.81

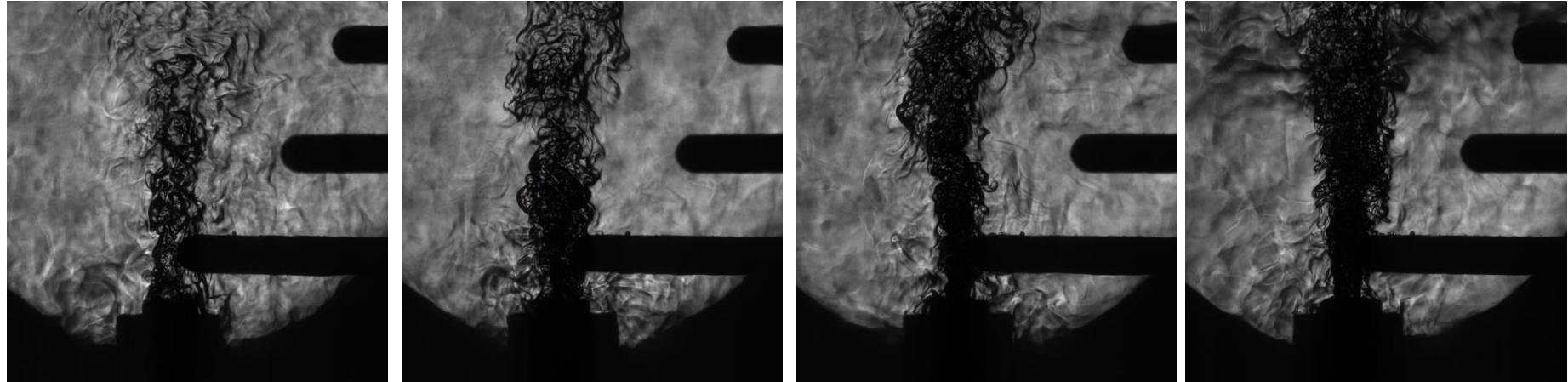
Re = 1780
F = 5.03

Re = 2680
F = 7.31

As Re increases, jet transitions from mostly laminar to turbulent

Classical Reynolds number transition to turbulence of jets

Supercritical Jet Injected into Subcritical Water



Re = 471
F = 0.5

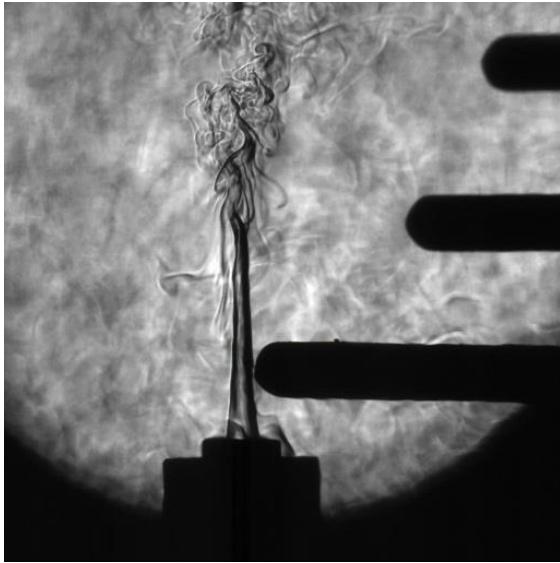
Re = 943
F = 1.0

Re = 1890
F = 2.0

Re = 2830
F = 3.0

Transition appears to be from turbulent buoyant plume to turbulent buoyant jet

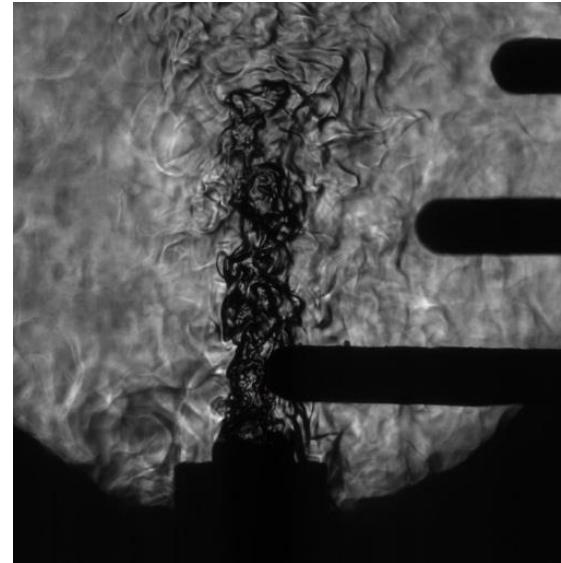
Jet Comparison



Supercritical into supercritical

$Re = 448$

$F = 1.37$



Supercritical into subcritical

$Re = 471$

$F = 0.5$

For similar Reynolds and Froude numbers the character of the two jets is strikingly different.

Property Variations near Critical Point

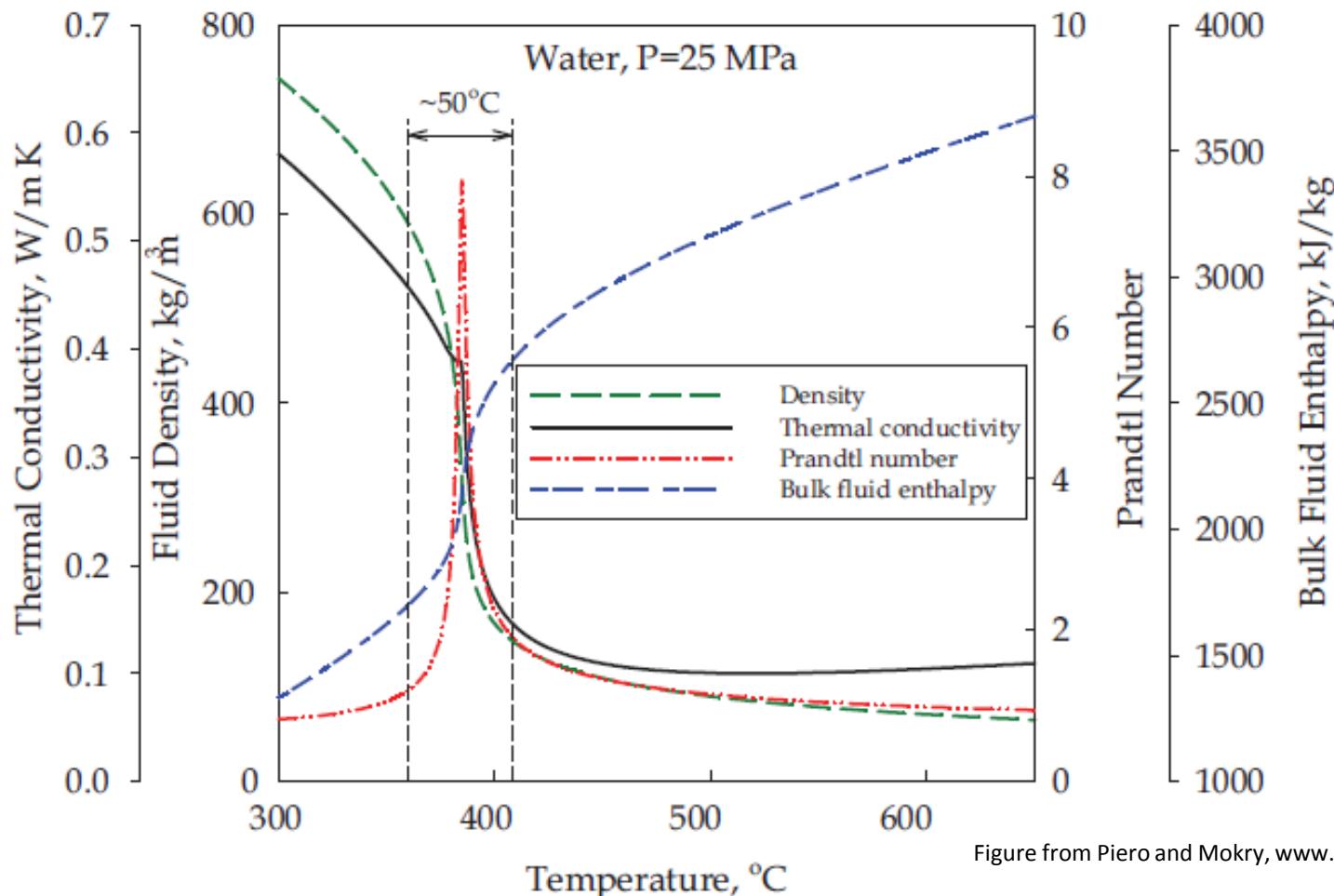


Figure from Piero and Mokry, www.intechopen.com

Influence of compressibility, C_p , λ ?

Vorticity Equation

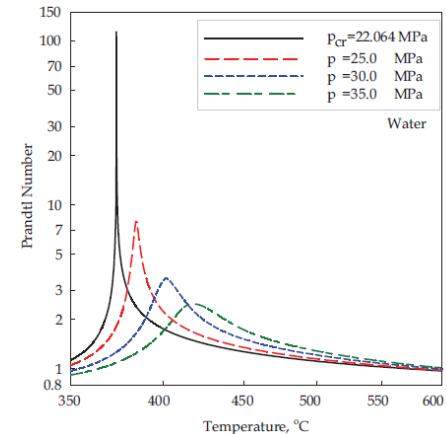
Consider azimuthal vorticity equation for axisymmetric, variable density with buoyancy flow.

Viscous effects not shown

$$\begin{aligned} V &= \nabla \times \psi + \nabla \varphi \\ \omega &= \nabla \times V = \nabla \times (\nabla \times \psi) \\ \nabla \cdot V &= \nabla^2 \varphi \end{aligned}$$

$$\frac{D\omega}{Dt} - \omega \frac{v_r}{r} + \omega(\nabla \cdot V) = \frac{1}{\rho^2} \left(\frac{\partial \rho}{\partial r} \frac{\partial p}{\partial x} - \frac{\partial p}{\partial r} \frac{\partial \rho}{\partial x} \right) - \frac{g}{\rho} \frac{\partial \rho}{\partial r}$$

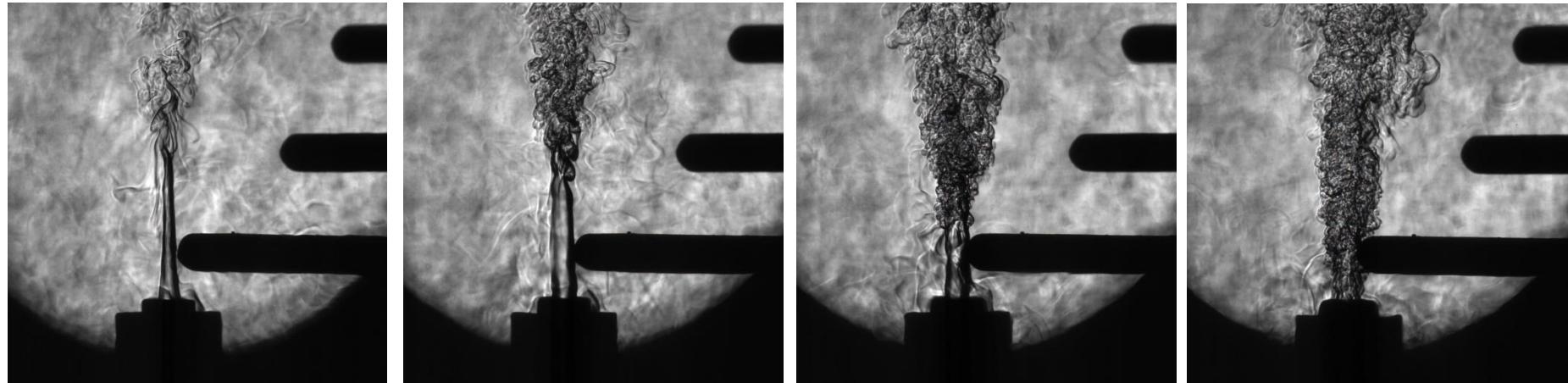
↓ ↓ ↓ ↓
 Vortex Compressibility Baroclinic Buoyancy
 Stretching $\sim M^2$ $\sim \text{Pr}$ $\sim \text{Pr}/F^2$



- Prandtl number ($\text{Pr} = \mu C_p / \lambda = \delta_v / \delta_T$) comes in because thermal mixing layer thickness can be much different (thinner) than velocity shear layer
Note $\text{Pr}/F^2 \sim \text{Ra}/\text{Re}^2$
- $M^2 \ll 1$ for the conditions of the experiment. It can be large very close to the critical point (speed of sound $\rightarrow 0$)

Supercritical Jet Injected into Supercritical Water

Transition from Buoyant Laminar Jet to Buoyant Turbulent Jet



Re = 448
 $\text{Pr}/F^2 = 1.4$

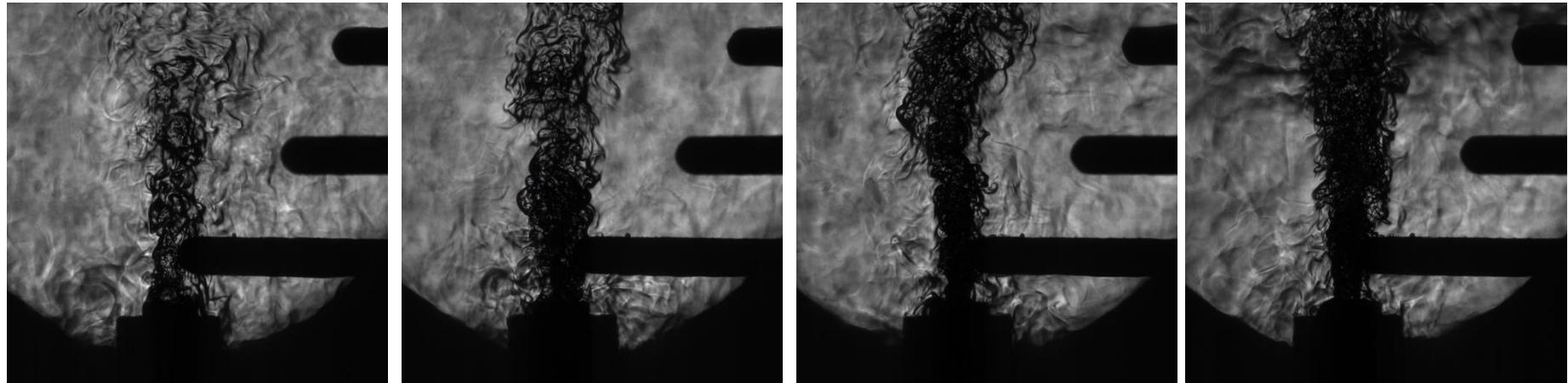
Re = 1330
 $\text{Pr}/F^2 = 0.2$

Re = 1780
 $\text{Pr}/F^2 = 0.11$

Re = 2680
 $\text{Pr}/F^2 = 0.05$

Supercritical Jet into Subcritical Water

Transition from Buoyant Turbulent Plume to Buoyant Turbulent Jet



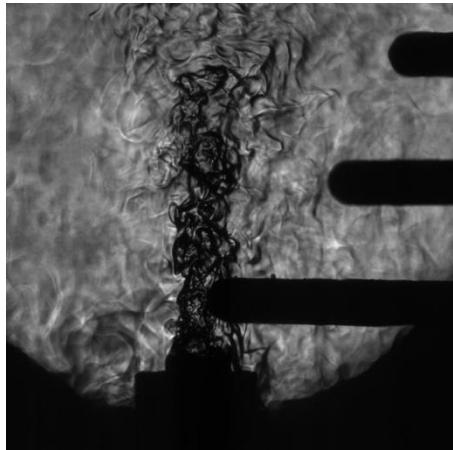
Re = 471
 $\text{Pr}/F^2 = 56$

Re = 943
 $\text{Pr}/F^2 = 14$

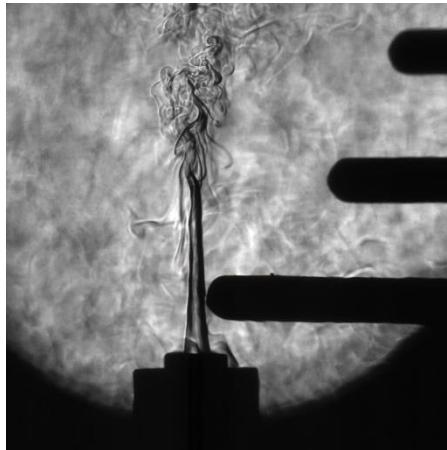
Re = 1890
 $\text{Pr}/F^2 = 3.5$

Re = 2830
 $\text{Pr}/F^2 = 1.6$

Findings



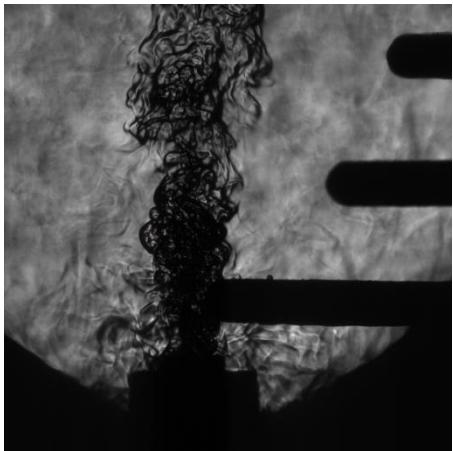
$Re = 471$
 $Pr/F^2 = 56$



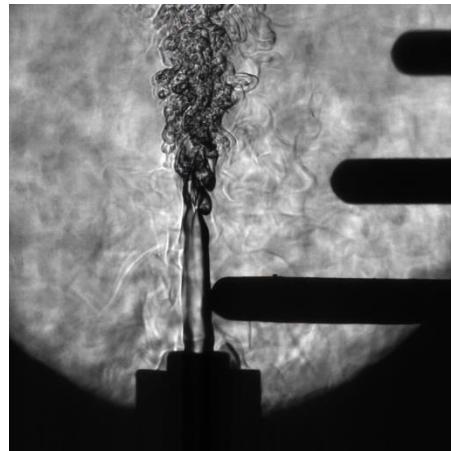
$Re = 448$
 $Pr/F^2 = 1.4$

At low Reynolds number, the parameter Pr/F^2 controls the laminar/turbulent nature of the jet . For values of the parameter $\gg 1$, the jet is turbulent due to strong buoyancy effect.

Findings (contd)



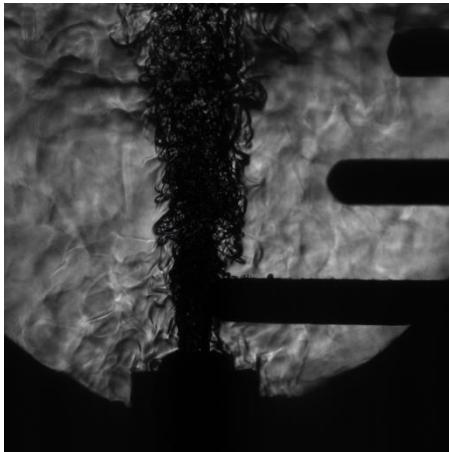
$Re = 943$
 $Pr/F^2 = 14$



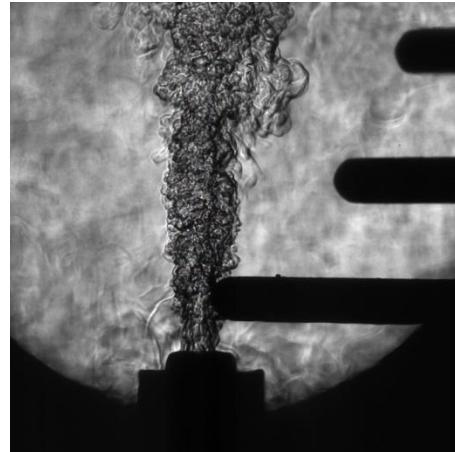
$Re = 1330$
 $Pr/F^2 = 0.2$

At intermediate Reynolds number the situation is similar to the low Reynolds number case.

Findings (contd 2)



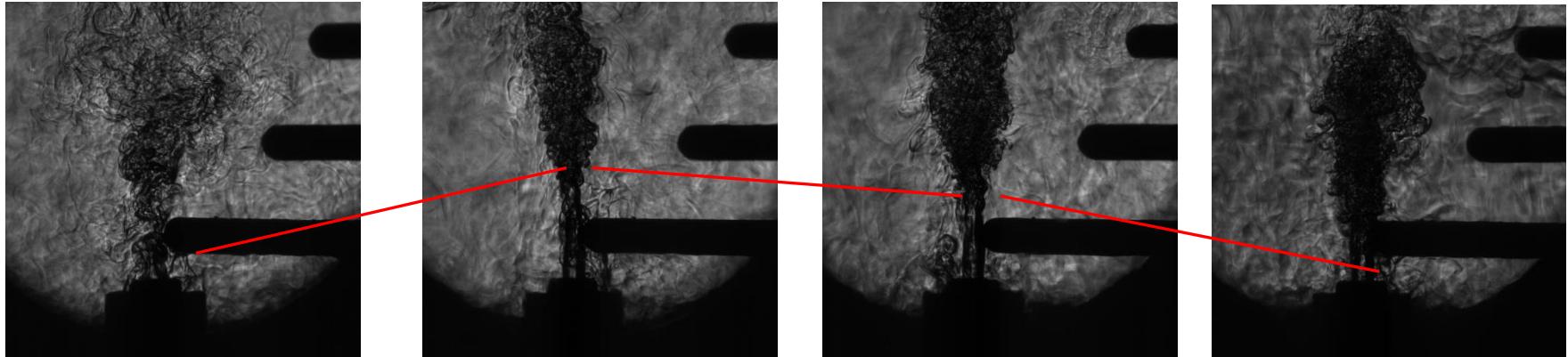
$Re = 2830$
 $Pr/F^2 = 1.6$



$Re = 2680$
 $Pr/F^2 = 0.05$

At large Reynolds numbers (> 2000), the jet is turbulent.

Supercritical Jet (~ 450 C) Injected into Transcritical Water (~ 380 C)



$Re = 466$
 $Pr/F^2 = 7$

$Re = 935$
 $Pr/F^2 = 1.2$

$Re = 1400$
 $Pr/F^2 = 0.6$

$Re = 1880$
 $Pr/F^2 = 0.4$

Note appearance of laminar length as flow transitions from plume to jet behavior

Summary

- Behavior of supercritical water jets injected into subcritical and supercritical was studied
- The laminar/turbulent nature of the jet under gravitational conditions depends upon the Reynolds number of injection and the parameter Prandtl number/(Froude number)²
- Compressibility may be important near the critical point but it is not clear it can be separated from gravity effects on the ground

Acknowledgments

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